IMPORTANT FORMULAE IN ELECTROSTATICS

1. **Electrostatic force between two charges**
   $F = K.\frac{q_1 q_2}{r^2} = \frac{1}{4\pi\epsilon_0\epsilon_r}.\frac{q_1 q_2}{r^2}$
   For air, $\epsilon_r = 1$
   Fair = $\frac{1}{4\pi\epsilon_0}.\frac{q_1 q_2}{r^2} = 9\times10^9\ \frac{q_1 q_2}{r^2}$
2. **Electric field intensity due to a point charge,** $\vec{E} = \lim_{q_0\to 0}\frac{\vec{F}}{q_o}$
3. **Electric field intensity due to infinite linear charge density (λ)**
   $E = \frac{1}{4\pi\epsilon_0}.\frac{2\lambda}{r}$
4. **Electric field intensity near an infinite thin sheet of surface charge density** σ
   $E = \frac{\sigma}{2\epsilon_0}$
   For thick sheet $= \frac{\sigma}{\epsilon_0}$ **.**
5. **Electric potential,** $V = \lim_{q_0\to 0}\frac{w}{q_o}$
   Electric potential due to a point charge, $V = \frac{1}{4\pi\epsilon_0}.\frac{q}{r}$
6. **Relation between electric field and potential** $E = -\frac{dV}{dr} = \frac{V}{r}$ **(numerically)**
7. **Dipole moment,** $\vec{P} = q.2\vec{l}$
8. **Torque on a dipole in uniform electric field,** $\vec{\tau} = \vec{p}\times\vec{E}$**.**
9. **Potential energy of dipole,** $\cup = -\vec{p}.\vec{E} = -pE\cos\theta$
10. **Work done in rotating the dipole in uniform electric field from orientation** Q_1 **to** Q_2 **is**
    $W = U_2 - U_1 = pE(\cos\theta_1 - \cos\theta_2)$
11. **Electric field due to a short dipole**
    (i) **at axial point,** $E_{axis} = \frac{1}{4\pi\epsilon_0}.\frac{2p}{r^3}$
    (ii) **at equatorial point,** $E_1 = \frac{1}{4\pi\epsilon_0}.\frac{p}{r^3}$
12. **Electric potential due to a short dipole**
    (i) **At axial point,** $V_{axis} = \frac{1}{4\pi\epsilon_0}.\frac{p}{r^2}$
    (ii) **At equatorial point,** $V = 0$**.**
13. **Dielectric constant,** $K = \frac{\epsilon}{\epsilon_0} = \frac{C_{med}}{C_{air}}$
14. **Capacitance of parallel plate capacitor**
    (i) $C = \frac{A\epsilon_0 K}{d}$ **, in medium of dielectric constant K**
    (ii) $C = \frac{A\epsilon_0}{d - t(1-\frac{1}{K})}$**; if space between plate partially filled with dielectric of thickness t.**
15. **Combination of capacitors :-**
    (i) **In series,** $\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$, $q_1 = q_2 = q_3$, $V = V_1 + V_2 + V_3$
    (ii) **In parallel,** C= $C_1 + C_2 + C_3$, $q = q_1 + q_2 + q_3$, $V_1 = V_2 = V_3 = V$
16. **Energy stored by capacitor**
    $\cup = \frac{1}{2}CV^2 = \frac{Q^2}{2C} = \frac{1}{2}QV$
17. **Electrostatic energy density**
    $\vartheta_e = \frac{1}{2}\epsilon_0 E^2$**, in air**
    $\vartheta_e = \frac{1}{2}\epsilon E^2$**, in medium**

18. Total electric flux, $\boldsymbol{\Phi = \oint \vec{E}.\overrightarrow{ds} = \frac{1}{\epsilon_0} \times net\ charge\ enclosed\ by\ the\ surface}$

NUMERICALS

LEVEL I

1. What is the charge acquired by a body when 1 million electrons are transferred to it?

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2. An attractive force of 5N is acting between two charges of +2.0 μC & -2.0 μC placed at some distance. If the charges are mutually touched and placed again at the same distance, what will be the new force between them?

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3. A charge of +3.0 x 10^{-6} C is 0.25 m away from a charge of -6.0 x 10^{-6}C.
   a. What is the force on the 3.0 x 10^{-6} C charge?
   b. What is the force on the -6.0 x 10^{-6} C charge?

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4. An electric dipole consist of a positive and a negative charge of 4μC each placed at a distance of 5mm. Calculate dipole moment.

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5. Three capacitors of capacitances 2μF, 3μF and 4μF are connected in parallel. What is the equivalent capacitance of the combination? Determine charge on each capacitor, if the combination is connected to 100V supply?

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6. An electric dipole with dipole moment 4x10^{-9}C-m is aligned at 30^0 with direction of electric field of magnitude 5x10^4N/C. Calculate the magnitude of the torque acting on the dipole.

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7. A point charge of 2μC is at the centre of cubic Gaussian surface 9.0 cm in edge. What is the net electric flux through the surface?

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8. What is the amount of work done in moving a 200nC charge between two points 5 cm apart on an equipotential surface?

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9. How much work must be done to charge a 24 μF capacitor, when the potential difference between the plates is 500 V?

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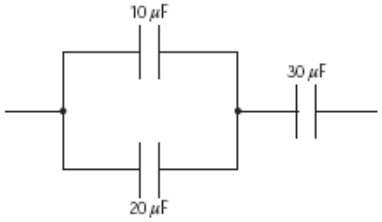
10. What is the equivalent capacity of the network given below?



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LEVEL II

1. What is the work done in moving a charge of 100μC through a distance of 1cm along the equatorial line of dipole?

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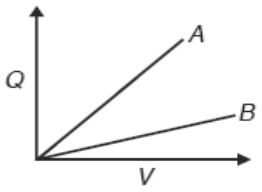
2. The given graph shows that variation of charge q versus potential difference V for two capacitors C_1 and C_2. The two capacitors have same plate separation but the plate area of C_2 is double than that of C_1. Which of the lines in the graph correspond to C_1 and C_2 and why?



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3. Two point charges 5μC and – 4 μC are separated by a distance of 1 m in air. At what point on the line joining the charges is the electric potential zero?

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4. Two charges +5μC and +20μC are placed 15 cm apart. At what point on the line joining the two charges is the electric field zero?

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5. Two charges +16μC and −9μC are placed 8 cm apart. At what point on the line joining the two charges is the electric field zero?

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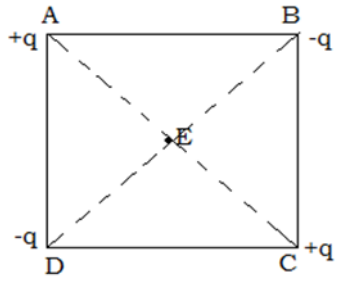
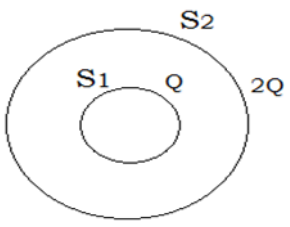
6. A 600 pF capacitor is charged by a 200 V supply. It is then disconnected and from the supply and is connected to another uncharged 600 pF capacitor. How much electrostatic energy is lost in the process.

7. Keeping the voltage of the charging source constant, what will be the percentage change in the energy stored in a parallel plate capacitor if the separation between its plates were to be decreased by 10%.

8. Four charges are placed at the vertices of a square of side d as shown in the figure.(i) Find the work done to put together this arrangement. (ii) A charge $q_0$is brought to the center E of the square, the four charges being held fixed at its corners. How much extra work is needed to do this?



9. If S_1 and S_2 are two hollow spheres enclosing charges Q and 2Q respectively as shown in the figure



(i) What is the ratio of the electric flux through S_1 and S_2?
(ii) How will the flux through the sphere S_1 change, if a medium of dielectric constant 5 is filled in the space inside S_1.

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10. A charge of 24μC is given to a hollow sphere of radius 0.2m. Find the potential
(i) at the surface of the sphere, and
(ii) at a distance of 0.1 m from the centre of the sphere.
(iii)at the centre

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UNIT: I ELECTROSTATICS

ANSWERS

LEVEL I

1. Q = Ne 1.6 $x10^{-13}$C
2. F=0
3. $F_{AB} = F_{BA}$=2.736N
4. P=$2x10^{-8}$ C-m
5.
6. 10^{-4}Nm
7. $2{,}26x10^{5}Nm^2/C$
8. W=0
9. W=3J
10. C=15μF

LEVEL II

1. 0
2. A
3. $\frac{5}{9}m$ from 5μC charge
4. 5 cm from 5 μC charge
5. 24cm from -9 μC charge
6. $6x10^{-6}$ J
7. 11.11%
8. $\frac{q^2}{4\pi\epsilon_0}(4-\sqrt{2})$, 0
9. $1:3,\ \emptyset = \frac{Q}{5\epsilon_0}$
10. (i) $1.08x10^{6}$V (ii) $1.08x10^{6}$V (iii)$1.08x10^{6}$V